A Fixed Point Interpretation of Pareto Optimization

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Abstract. Pareto optimization is shown to be equivalent to a fixed point problem for a certain multivalued function. This viewpoint provides a solution procedure for some problems.

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